A sequence whose adjacent terms always make the given algebraic expression a square number

written by 200007 1016 on Functor Network original link: https://functor.network/user/942/entry/436

$$\frac{1 - 36z + 23z^2}{1 - 38z + 38z^2 - z^3} = \sum_{i=0}^{\infty} a_i z^i$$
 (1)

$$3 + \frac{a_i^3 + a_{i+1}^3}{\frac{1}{a_i} + \frac{1}{a_{i+1}}} = (6a_i a_{i+1} - 6 - a_i - a_{i+1})^2$$
 (2)