

[DC #1]

Anabolic Hilbert • 16 Feb 2025

[Differential Calculus - FME Q2 2024-2025]

<Post 1>

Proof that (\mathbb{R}^n, d_2) is a metric space is done.

I've struggled to show $d_2(x, y) \leq d_2(x, z) + d_2(z, y)$. As this definition:

$$d_2(x, y) := \sqrt{\sum_{i=1}^n (x_i - y_i)^2}$$

.

Was hard to grasp to me, as for the usual style of teaching this was presented just symbolically and nothing behind that. So I started the proof forgetting that square root.

Then I also did a mistake using the CBS-Inequality, as the same thing. The inequality was introduced as a symbolical painting. So guess what, I forgot the square on the LHS.

Once that was fixed, (also did some examples in \mathbb{R}^2), the proof worked out well.

Writing the whole proof out with the subindexes was very exhausting.

I wonder if my classmates associate this d_2 with something or just do this proof on memory force.

However, it's done.

Going for a run now.